## Warm-Up

Take out your HW.
Find each measure.


## Fun Fact

The tracks on a roller coaster have triangular reinforcements between the tracks for support and stability. The triangular supports in the photo are isosceles triangles.


# Essential Skill 2: Congruent Triangles 

LT 2.3 Isosceles and Equilateral Triangles

## Learning Objective

## I will be able to . . .

* Use properties of isosceles triangles.
* Use properties of equilateral triangles.


## Glossary

## LT 2.3 Glossary: Isosceles Triangle

This is an alphabetical list of the key vocabulary terms you will learn.
As you study the learning target, remember to review the vocabulary before the exams.

| Vocabulary Term | Definition/Description/Example | Drawing |
| :--- | :---: | :---: |
| Isosceles | Has at least 2 congruent sides. |  |
| Triangle |  |  |



## Glossary

## LT 2.3 Glossary: Theorems

This is an alphabetical list of the key vocabulary terms you will learn.
As you study the learning target, remember to review the vocabulary before the exams.

| Vocabulary Term | Definition/Description/Example |
| :--- | :--- | :--- |
| Isosceles Triangle |  |
| Theorem |  |$\quad$| If two sides of a triangle are |
| :--- |
| congruent, then the angles |
| opposite those sides are |
| congruent. |$\quad$ Drawing

## Example 1a

Name two unmarked congruent angles. J ustify your answer.
$<\mathrm{ACB}$ is opposite AB
$<\mathrm{B}$ is opposite AC
$\angle \overrightarrow{A C B} \cong \angle B$.

$\overline{A D}$ is opposite $\angle A C D$
$\overline{A C}$ is opposite $\angle D$.
$\overline{\overline{A D}} \cong \overline{A C}$.

## Example 1b

Name two unmarked congruent segments.
J ustify your answer.


## Example 1c

Name two unmarked congruent angles. J ustify your answer.


Name two unmarked congruent segments.
J ustify your answer.

## Glossary

## LT 2.3 Glossary: Equilateral Triangle

This is an alphabetical list of the key vocabulary terms you will learn.
As you study the learning target, remember to review the vocabulary before the exams.

| Vocabulary Term | Definition/Description/Example | Drawing |
| :---: | :---: | :---: |
| Equilateral Triangle | 3 congruent sides |  |
| Corollary 2.3a | A triangle is equilateral if and only if it is equiangular. <br> Example If $\angle A \cong \angle B \cong \angle C$, then $\overline{A B} \cong \overline{B C} \cong \overline{C A} .$ |  |
| Corollary 2.3 b | Each angle of an equilateral triangle measures $60^{\circ}$. $\begin{aligned} & \text { Example If } \overline{D E} \cong \overline{E F} \cong \overline{F E}, \text { then } \\ & \\ & m \angle A=m \angle B=m \angle C=60 . \end{aligned}$ |  |

## Example 2a

Find $\boldsymbol{m} \angle \boldsymbol{Y}$ J ustify your answer.

Answer:

$$
m \angle X+m \angle Y+m \angle Z=180
$$

$$
60+m \angle Y+m \angle Y=180
$$

$$
60+2(m \angle Y)=180
$$

$$
2(m \angle Y)=120
$$

$$
m \angle Y=60
$$



## Triangle Sum Theorem

$m \angle X=60, m \angle Z=m \angle Y$
Simplify.
Subtract 60 from each side.
Divide each side by 2.

## Example 2b

## Find YZ J ustify your answer.

Answer:

$m \angle Z=m \angle Y$, so $m \angle Z=60$ by substitution. Since $m \angle X=60$, all three angles measure 60, so the triangle is equiangular. Because an equiangular triangle is also equilateral, $X Y=X Z=Z Y$. Since $X Y=8$ inches, $Y Z=8$ inches by substitution.

## Example 2c

Find $m \angle M$
J ustify your answer.


Answer:

## Example 2d

Find PN
J ustify your answer.


Answer:

## Example 3a

Find the value of each variable. Justify your answer.

Answer:


$$
\begin{aligned}
A B & =B C & & \text { Definition of equilateral triangle } \\
3 & =4 y-5 & & \text { Substitution } \\
8 & =4 y & & \text { Add } 5 \text { to each side. } \\
2 & =y & & \text { Divide each side by } 4 .
\end{aligned}
$$

## Example 3a

Find the value of each variable. J ustify your answer.


Answer:

$$
x=7, y=2
$$

## Homework

Class: Complete Skills Practice - \#1-8 all

Honors: Complete Honors Skills Practice

- all except \#10

