

LT 1.2 Study Guide and Intervention

Angles and Parallel Lines: Proofs

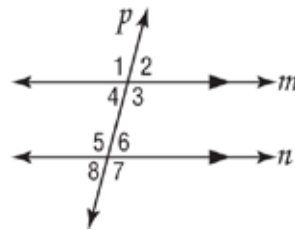
Parallel Lines and Angle Pairs When two parallel lines are cut by a transversal, the following pairs of angles are congruent.

- corresponding angles
- alternate interior angles
- alternate exterior angles

Also, consecutive interior angles are supplementary.

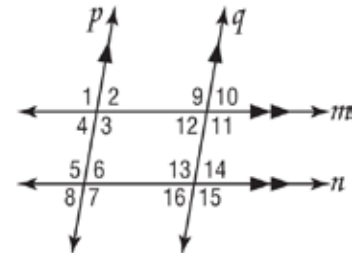
Example: In the figure, $m \angle 2 = 75$. Find the measures of the remaining angles.

- | | |
|--------------------|--|
| $m \angle 1 = 105$ | $\angle 1$ and $\angle 2$ form a linear pair. |
| $m \angle 3 = 105$ | $\angle 3$ and $\angle 2$ form a linear pair. |
| $m \angle 4 = 75$ | $\angle 4$ and $\angle 2$ are vertical angles. |
| $m \angle 5 = 105$ | $\angle 5$ and $\angle 3$ are alternate interior angles. |
| $m \angle 6 = 75$ | $\angle 6$ and $\angle 2$ are corresponding angles. |
| $m \angle 7 = 105$ | $\angle 7$ and $\angle 3$ are corresponding angles. |
| $m \angle 8 = 75$ | $\angle 8$ and $\angle 6$ are vertical angles. |



Exercises

In the figure, $m \angle 3 = 102$. Find the measure of each angle.
Tell which postulate(s) or theorem(s) you used. Use a two column-proof.



1. 5

2. 6

3. 11

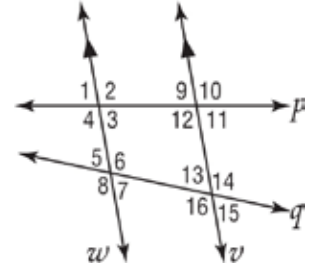
4. 7

5. 15

LT 1.2 Study Guide and Intervention

Angles and Parallel Lines: Proofs

In the figure, $m \angle 9 = 80$ and $m \angle 5 = 68$. Find the measure of each angle. Tell which postulate(s) or theorem(s) you used. Use a two column proof.



7. $\angle 12$

8. $\angle 1$

9. $\angle 4$

10. $\angle 3$

11. $\angle 7$

12. $\angle 16$

LT 1.2 Study Guide and Intervention (continued)

Angles and Parallel Lines

Algebra and Angle Measures Algebra can be used to find unknown values in angles formed by a transversal and parallel lines.

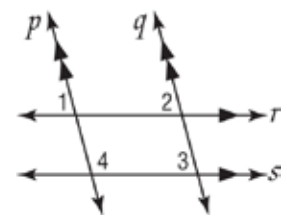
Example: If $m \angle 1 = 3x + 15$, $m \angle 2 = 4x - 5$, and $m \angle 3 = 5y$, find the value of x and y .

$p \parallel q$, so $m \angle 1 = m \angle 2$
because they are corresponding angles.

$$\begin{aligned}
 m \angle 1 &= m \angle 2 \\
 3x + 15 &= 4x - 5 \\
 3x + 15 - 3x &= 4x - 5 - 3x \\
 15 &= x - 5 \\
 15 + 5 &= x - 5 + 5 \\
 20 &= x
 \end{aligned}$$

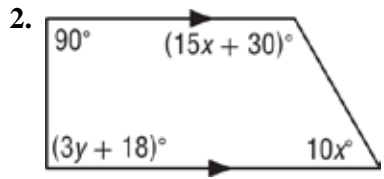
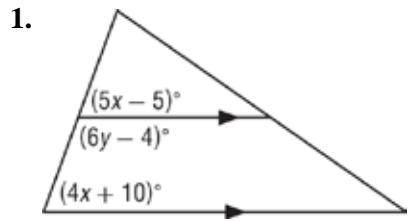
$r \parallel s$, so $m \angle 2 = m \angle 3$
because they are corresponding angles.

$$\begin{aligned}
 m \angle 2 &= m \angle 3 \\
 75 &= 5y \\
 \frac{75}{5} &= \frac{5y}{5} \\
 15 &= y
 \end{aligned}$$



Exercises

Find the value of the variable(s) in each figure. Explain your reasoning (Justify)

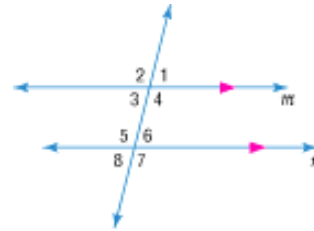


LT 1.2 Angles and Parallel Lines

Example 1: Use Corresponding Angles Postulate

In the figure, $m\angle 8 = 121$. Find the measure of each angle. Tell which postulates (or theorems) you used. Use a two column proof.

a. $\angle 3$

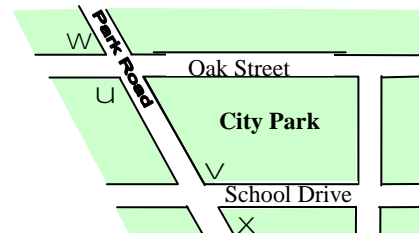


b. $\angle 1$

Real-World Example 2: Use Theorems about Parallel Lines

MAPS School Drive and Oak Street are parallel streets that intersect Park Road along the west side of City Park.

If $m\angle 1 = 122$, find $m\angle 2$. Use a two column proof.

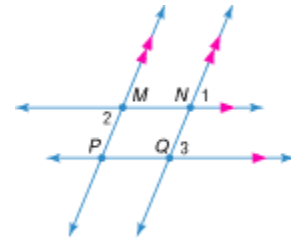


Example 3: Find Values of Variables

ALGEBRA Use the figure at the right to find the indicated variable. Explain your reasoning (Justify your answer)

If $m\angle 1 = 16x - 8$, $m\angle 2 = 4(y + 8)$, and $m\angle 3 = 14x + 2$, find x and y .

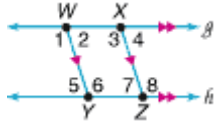
a. If $m\angle 1 = 16x - 8$, $m\angle 2 = 4(y + 8)$, and $m\angle 3 = 14x + 2$, find x .



b. If $m\angle 1 = 16x - 8$, $m\angle 2 = 4(y + 8)$, and $m\angle 3 = 14x + 2$, find y

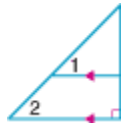
LT 1.2 Angles and Parallel Lines

1. Find the measure of $\angle 2$ if $g \parallel h$, $\overline{WY} \parallel \overline{XZ}$, and $m\angle 5 = 70$.



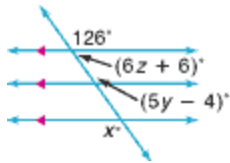
- | | |
|-----------------------------|------------------------------|
| <input type="checkbox"/> 60 | <input type="checkbox"/> 110 |
| <input type="checkbox"/> 70 | <input type="checkbox"/> 65 |

2. Find the measure of $\angle 2$ if $m\angle 1 = 8y - 6$ and $m\angle 2 = 7y$.



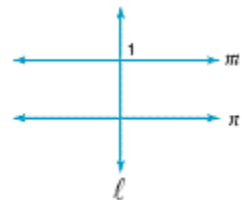
- | | |
|-----------------------------|-----------------------------|
| <input type="checkbox"/> 56 | <input type="checkbox"/> 49 |
| <input type="checkbox"/> 35 | <input type="checkbox"/> 42 |

3. What is the value of y ?



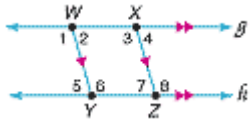
- | | |
|-----------------------------|-----------------------------|
| <input type="checkbox"/> 24 | <input type="checkbox"/> 30 |
| <input type="checkbox"/> 26 | <input type="checkbox"/> 28 |

4. If line m and n are parallel and l is perpendicular to m , then _____.



- | | |
|--|--|
| <input type="checkbox"/> l and n are skew lines. | <input type="checkbox"/> m is parallel to n . |
| <input type="checkbox"/> l is parallel to n . | <input type="checkbox"/> l is perpendicular to n . |

5. In the picture, if $m\angle 2 = 8x + 8$ and $m\angle 6 = 4x + 28$, what is $m\angle 2$?



76

96

90

104